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Ph.D Admission Test  
Sample Question Paper  
Computer Science and Engineering

### SAMPLE QUESTION PAPER

**Objective:** The focus of our admission test is to test your aptitude for research and problem solving skills.

#### Data Structures and Algorithm (Common for ECE and CSE)

1. What is the solution to the recurrence  $T(n) = T(n - 1) + 2$ ,  $T(1) = 2$
2. Solve:  $T(n) = 4T(n/2) + n \log n$ ,  $T(1) = 1$ .
3. Say True or False.
  - $3n^2 + 4n + 1 = O(n^3)$
  - $n + 1 = \Omega(\log n)$
  - $n = \Omega(n^2)$
  - $n^2 + 1 = O(n)$
4. The worst-case time to search an element in a binary heap of height  $h$  with  $n$  elements is  $O(n)$ .
5. Given a binary tree with  $l$  leaves, find the number of internal nodes (including root) as a function of  $l$ .
6. Let  $A$  be a sorted linked list and  $A'$  be an unsorted linked list. Inserting an element  $x$  into  $A$  (the resultant  $A$  must still be a sorted list) is efficient than inserting  $x$  into  $A'$ . Say True or false.

#### Computer Organization (Common for ECE and CSE)

1. True or False: Addition of a non-negative number with a negative number will never generate a carry.
2. The following three lines of *partial* code is expected to swap two variables. Complete the code. (i)  $a = a \text{ xor } b$  (ii)  $b = b \text{ xor } a$  (iii)...
3. Perform Booth's Multiplication:  $1\ 0\ 1\ 0\ 0\ 1\ 0\ 1 \times 1\ 1\ 1$
4. Identify the errors in the following code (it assumes 8085 instruction set)
  - MOV A,B
  - LOAD C,2000
  - MOV D,3000
  - MOV 2500,A
5. For the following specification with set associative mapping strategy, identify the number of bits in fields **Tag**, **set**, and **word**.
  - Cache size: 64 KB    RAM size: 512 MB    Block size: 4 KB    Word size: 4 Bytes
  - 4-way Set-associative mapping

#### Programming/Algorithms (Common for ECE and CSE)

1. In the following Pseudo code, how many times the statements *for* and *print* are executed.

```
void fprint()
```

```

    { for int i=1 to 5
      print i;
    }

```

- Write a recursive program to print all permutations of a finite set.
- Is it possible to write a C-program to print the set of natural numbers. Is it possible to write a C-program to print the set of Real numbers. Justify.
- At the termination of the following program, what is the value of *count*.

```

int n; /*-- Input n--*/
count-function()
int i=1, count=0;
while (i ≤ n)
{
i = i * 2;
count ++;
}

```

- Given a finite array  $A$ , the function  $\text{SWAP}(A[i], A[j])$  swaps the contents of  $A[i]$  with  $A[j]$  (Assume that the array is passed by reference). How do you use  $\text{SWAP}$  to reverse the contents of  $A$ .

#### **Discrete Mathematics** (For CSE only)

- Let  $A = \{1, 2, 3\}$  and  $R = \{(1, 2), (1, 3)\}$  be a binary relation defined on  $A$ . Is  $R$  transitive?
- Let  $A = \{1, 2\}$  and  $R = \{(1, 1), (2, 2)\}$  be a binary relation defined on  $A$ . Professor  $X$  says  $R$  is an equivalence relation. Is Professor  $X$  right?
- Count the number of permutations of the letters in 'admission'.
- Two logical statements  $S1$  and  $S2$  are defined as follows:  $S1$ : If  $3+2=5$ , then it rains on Sunday.  $S2$ :  $3+2=5$ . What logical inferences can you make from  $S1$  and  $S2$ .
- Count the number of one-one functions and onto functions (Assume the size of domain is  $m$  and the codomain is  $n$ ).

#### **Digital Signal Processing** (For ECE only)

- Given  $f \otimes g$  and also  $g$ , how do you find  $f$ ? where  $\otimes$  means convolution.
- What is the difference between convolution and correlation?
- Is mean filter linear? Justify your answer.

## Detailed Syllabus (Common for ECE and CSE)

**Data Structures:** ADT, Lists, Heaps, Binary trees, Graphs.

**Algorithms:** Time-complexity Analysis, solving recurrence relations, searching, sorting, algorithm design paradigms, basics of NP-completeness.

**Computer Organization:** Fixed/Floating point addition/subtraction/multiplication/division, addressing modes, cache memory (placement/replacement algorithms), pipelining, and hazards.

**C-Programming:** Iterative and recursive programs, structures, and pointers

**Discrete Mathematics:** (For CSE only) Sets, Relations, Functions, Counting, and First Order Logic, Proof Techniques, Automata theory.

**Digital Signal Processing (For ECE only)** Signals and Systems, transformations, filters, processor architectures, 2-D signal processing.